



Second Generation MethylMethAcrylate

*Concepts of Chemical Recycling:
Part 1*

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**MMAtwo
workshop**

15/09/2020

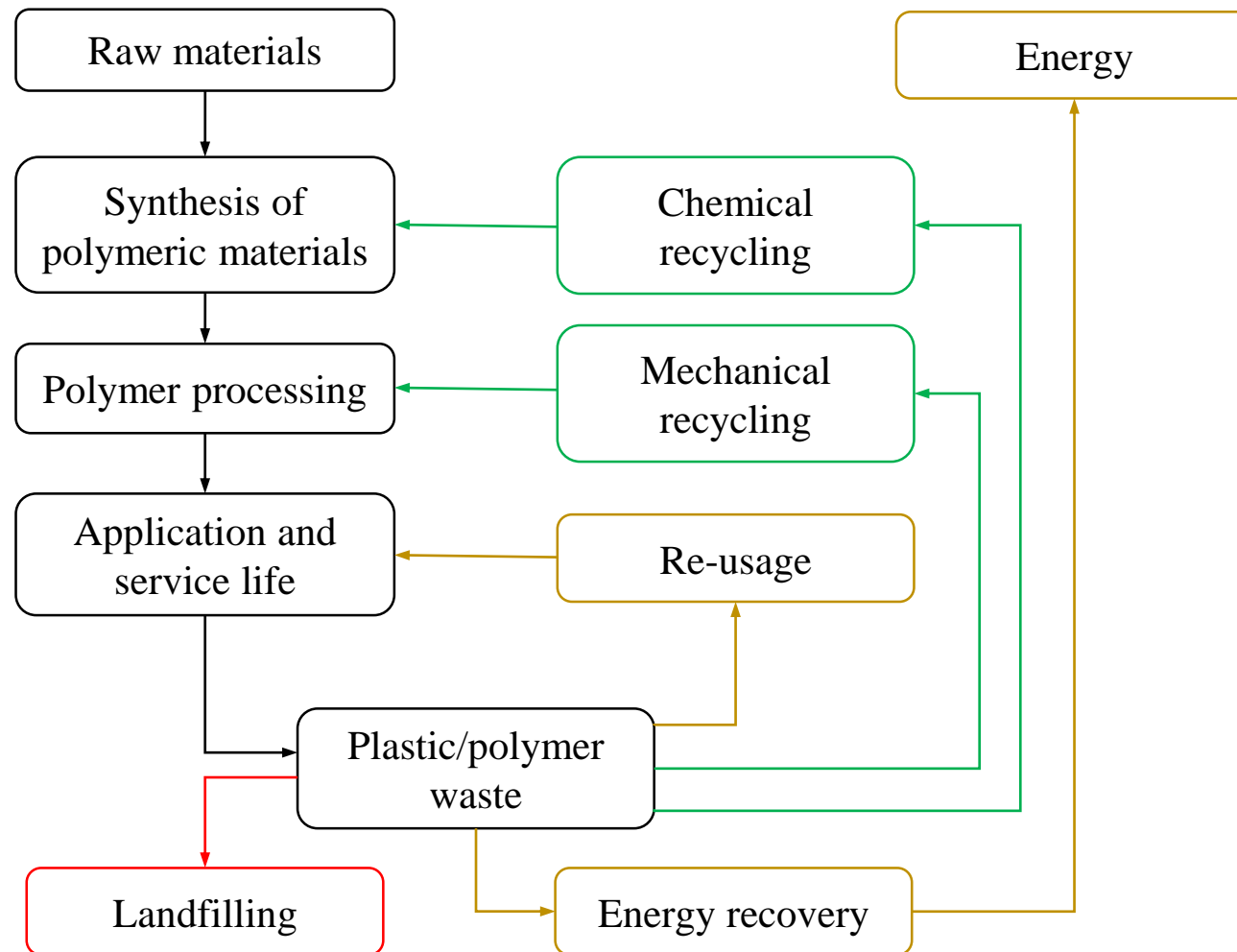
DOI: 10.13140/RG.2.2.36058.98241



This project has received funding from the European Union's Horizon 2020 research and innovation program under grant agreement N° 820687.
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Introduction



Outline

- Introduction
- Overview of depolymerization kinetic models
- Application of matrix based kinetic Monte Carlo to PMMA depolymerization
 - The role of defects & functionalities to initiate depolymerization
 - How defects & functionalities are introduced during free radical polymerization
 - Modeling of free radical polymerization
 - Modeling of depolymerization
- Conclusions



Depolymerization kinetic models

- Global conversion based models
- Global average chain length based models
- Elementary reaction step based models



Global conversion based models

$$\frac{d\alpha}{dt} = kf(\alpha) = A \exp\left(-\frac{E}{RT}\right) f(\alpha)$$

α : conversion

$$\frac{d\alpha}{dT} = \frac{A}{\beta} \exp\left(-\frac{E}{RT}\right) f(\alpha)$$

$$\frac{d\alpha}{dt} = \frac{d\alpha}{dT} \frac{dT}{dt} = \frac{d\alpha}{dT} \beta$$

$$\ln\left(\beta \frac{d\alpha}{dT}\right) = \ln[A f(\alpha)] - \frac{E}{RT}$$

$$\left[\frac{d \ln\left(\frac{d\alpha}{dT}\right)}{d\left(\frac{1}{T}\right)} \right]_{\alpha} = -\left[\frac{E}{R} \right]_{\alpha} + \left[\frac{d \ln(f(\alpha))}{d\left(\frac{1}{T}\right)} \right]_{\alpha}$$



Depolymerization kinetic models

- Global conversion based models

$$\left[\frac{d \ln \left(\frac{d\alpha}{dT} \right)}{d \left(\frac{1}{T} \right)} \right]_{\alpha} = - \left[\frac{E}{R} \right]_{\alpha} + \left[\frac{d \ln(f(\alpha))}{d \left(\frac{1}{T} \right)} \right]_{\alpha}$$

- Global average chain length based models

$$\ln \left(1 - \frac{1}{x_{n,0}} \right) - \ln \left(1 - \frac{1}{x_n} \right) = k_{ir} t$$

- Elementary reaction step based models

- Deterministic

- Stochastic



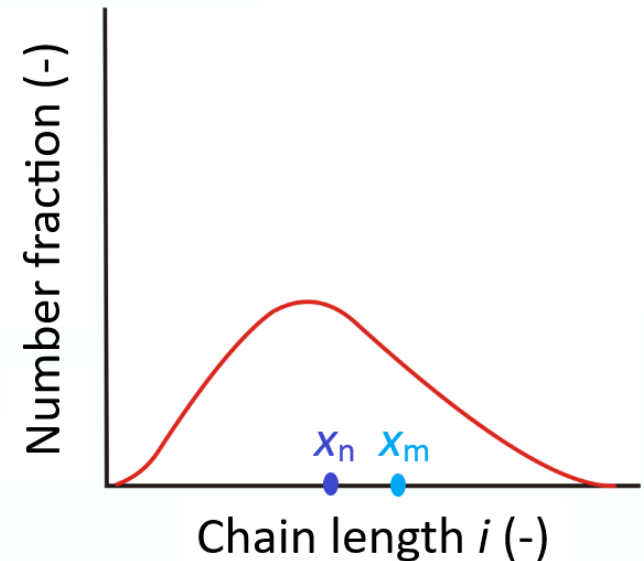
Deterministic elementary reaction based models

Population balances

$$\frac{d[P_i]}{dt} = -(i-1)k_f[P_i] + \dots \quad i = 1, i_{max}$$

Balances for moments only

$$\frac{d\mu_m}{dt} = -k_f(\mu_{m+1} - \mu_m) + \dots \quad m = 0, 1, 2$$



$$x_n = \frac{\mu_1}{\mu_0} \quad x_m = \frac{\mu_2}{\mu_1} \quad \mathcal{D} = \frac{x_m}{x_n}$$



Depolymerization kinetic models

- Global conversion based models

$$\left[\frac{d \ln \left(\frac{d\alpha}{dT} \right)}{d \left(\frac{1}{T} \right)} \right]_{\alpha} = - \left[\frac{E}{R} \right]_{\alpha} + \left[\frac{d \ln(f(\alpha))}{d \left(\frac{1}{T} \right)} \right]_{\alpha}$$

- Global average chain length based models

$$\ln \left(1 - \frac{1}{x_{n,0}} \right) - \ln \left(1 - \frac{1}{x_n} \right) = k_{ir} t$$

- Elementary reaction step based models

- Deterministic

- Stochastic

- ✓ Tree based kinetic Monte Carlo

- ✓ Matrix based kinetic Monte Carlo



Stochastic elementary reaction based models

- Stochastic sampling of reactions via kinetic Monte Carlo (kMC)
- Probability P to sample reaction v is proportional to its microscopic reaction rate R [s^{-1}]

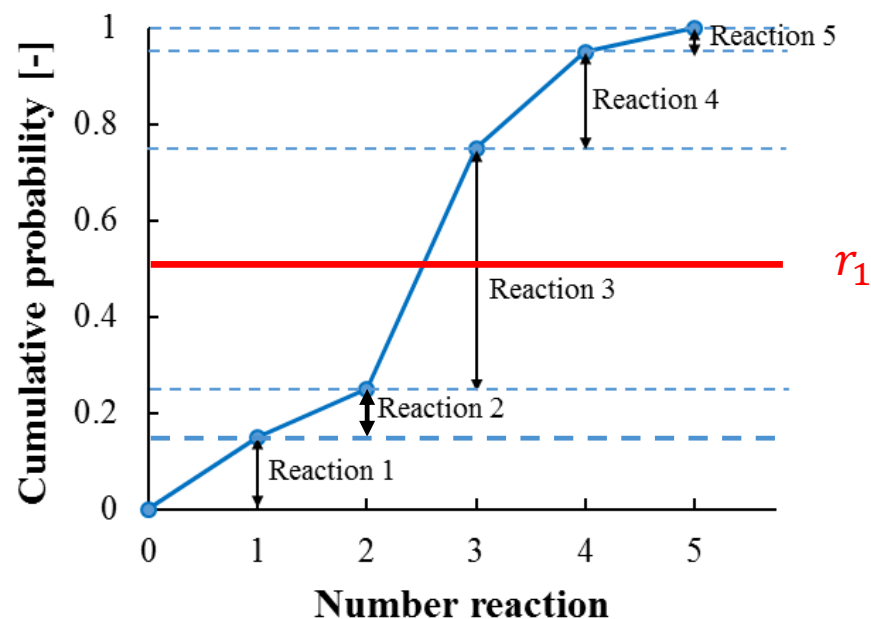
$$R(v) = k_{app,MC}^v n_A n_B$$

$$P(v) = R(v) \left[\sum_v R(v) \right]^{-1}$$

$$\sum_{v=1}^{v=\mu-1} P(v) < r_1 \leq \sum_{v=1}^{v=\mu} P(v)$$

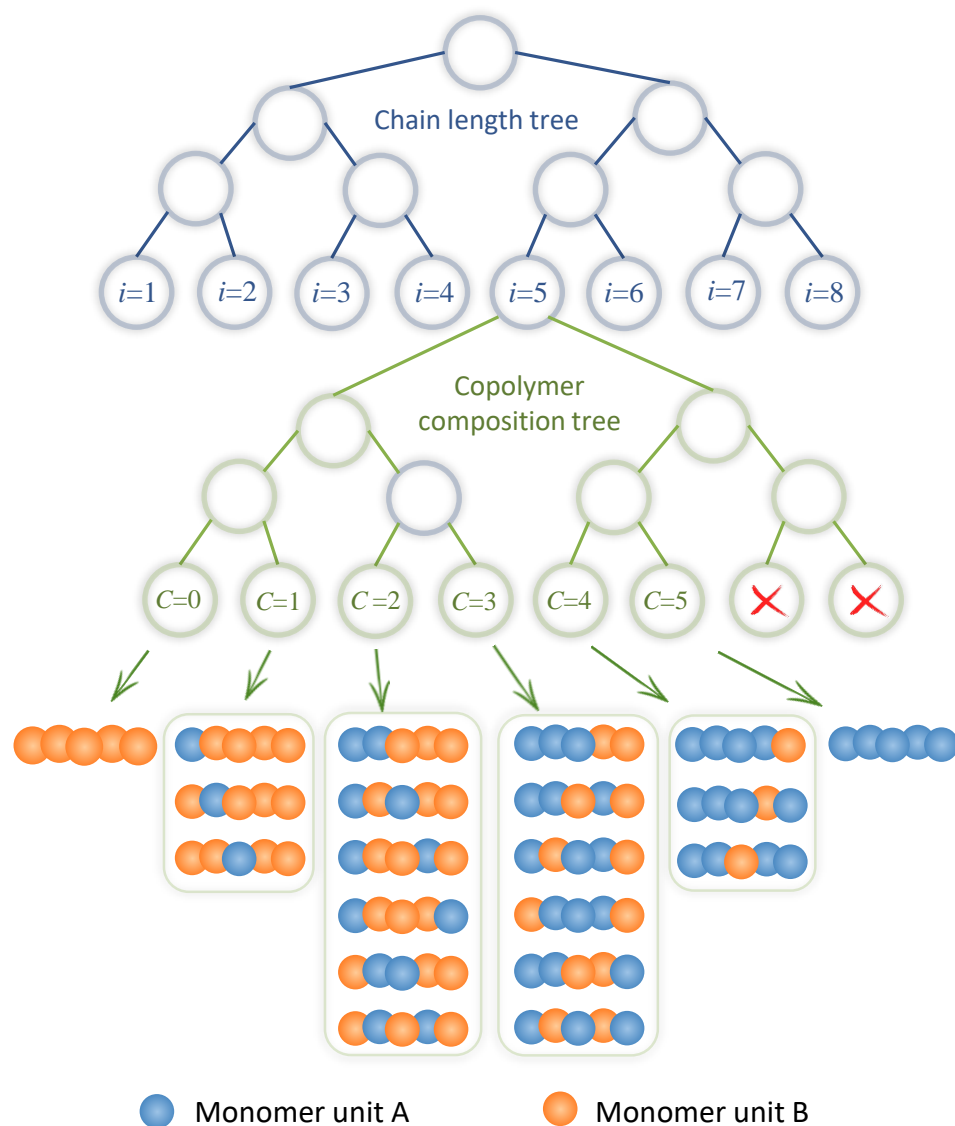
- Update of reaction time via

$$t = t + \frac{\ln\left(\frac{1}{r_2}\right)}{\sum_v R(v)}$$



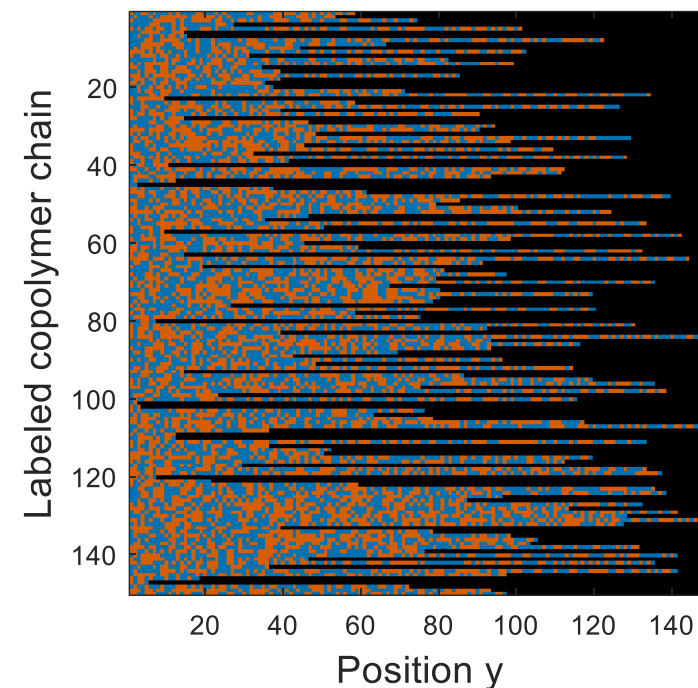
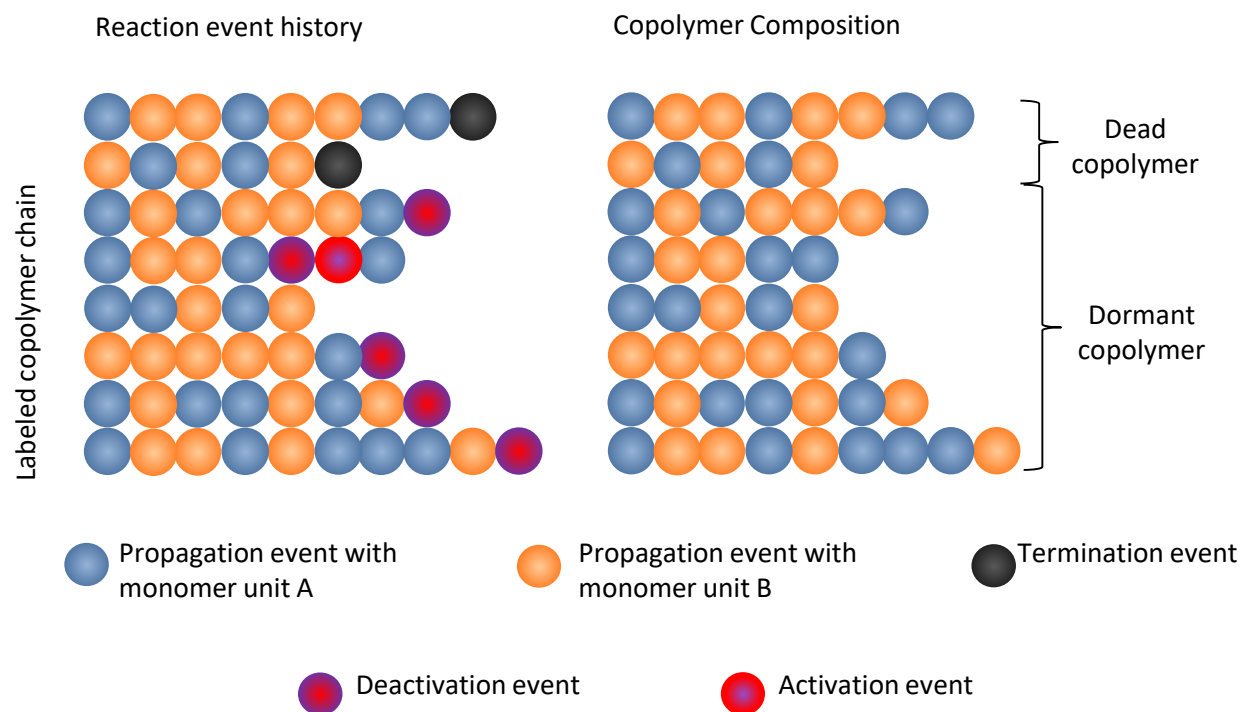


Tree based kMC





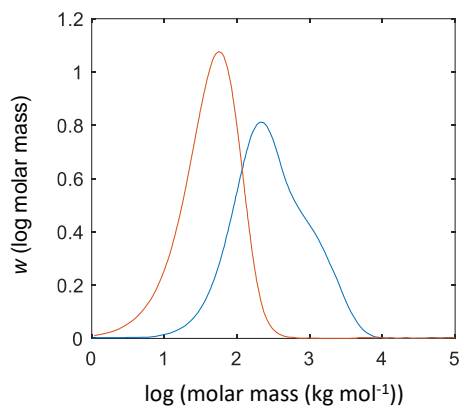
Matrix based kMC



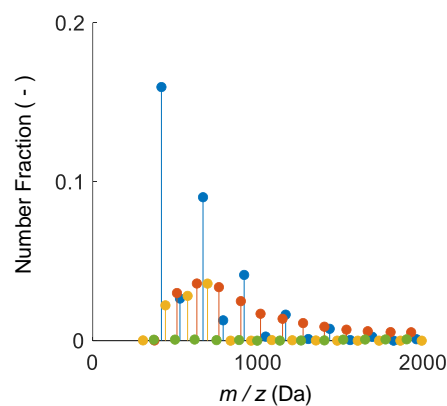


Tree vs. matrix based *k*MCMC

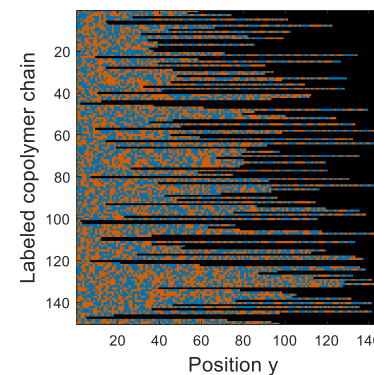
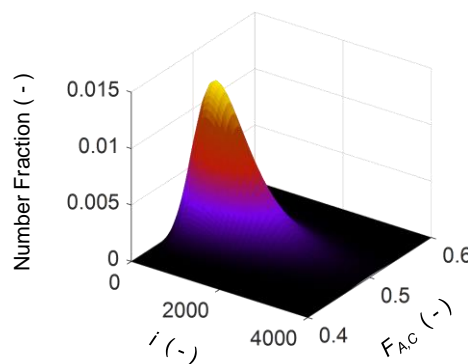
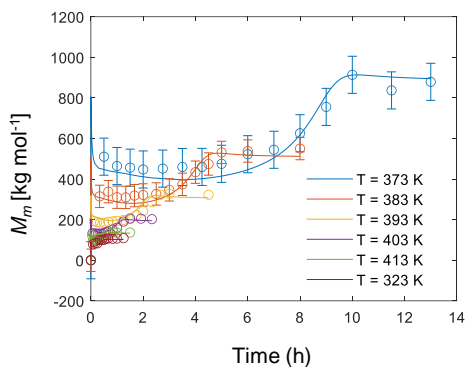
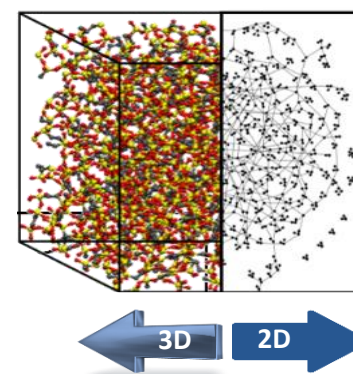
Univariate tree based



Bivariate tree based



Matrix based



Complexity and macromolecular structural detail

Outline

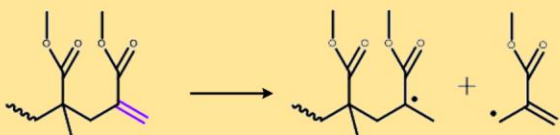
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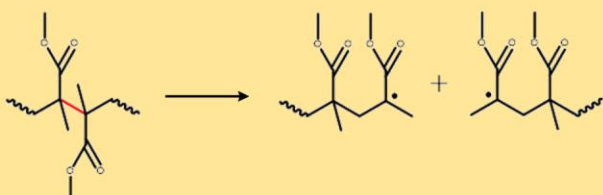
PMMA depolymerization reactions

Degradation initiation reactions

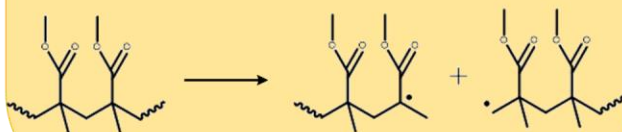
1) fission at unsaturated chain end



2) fission at head-to-head defect in a saturated chain

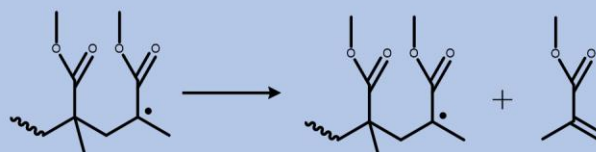


3) head-to-tail fission in a saturated chain



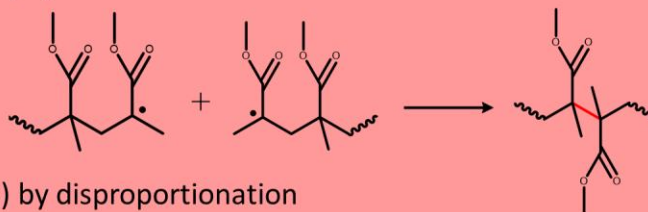
Depropagation reaction (unzipping)

β -scission

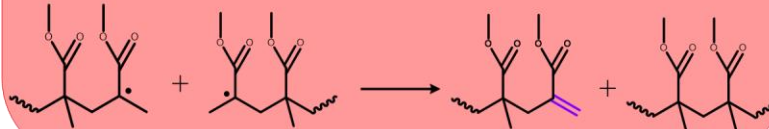


Termination reactions

1) by recombination



2) by disproportionation

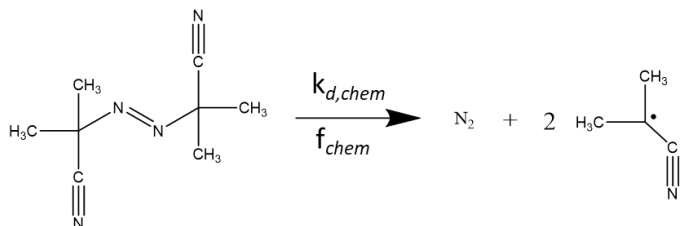


Initiation of depolymerization depends on the presence of structural defects and functionalities → also chain-by-chain visualization of polymerization needed

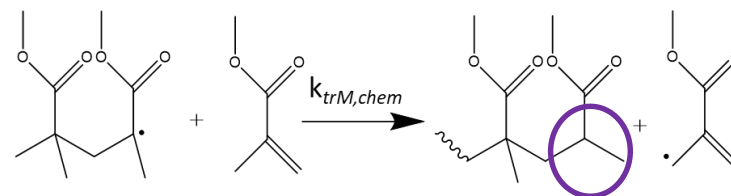


MMA free radical polymerization reactions

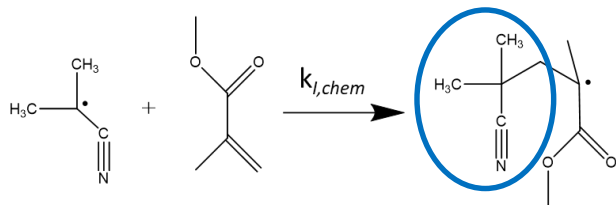
Initiator dissociation



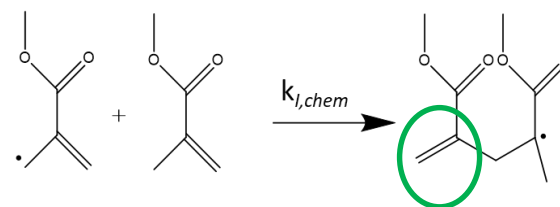
Chain transfer to monomer



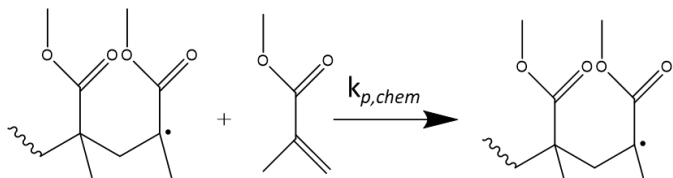
Chain initiation initiator radical



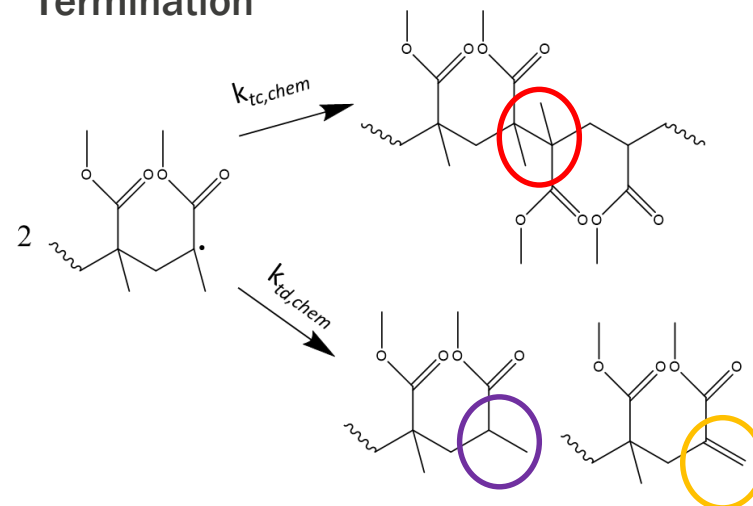
Chain initiation monomeric radical



Propagation



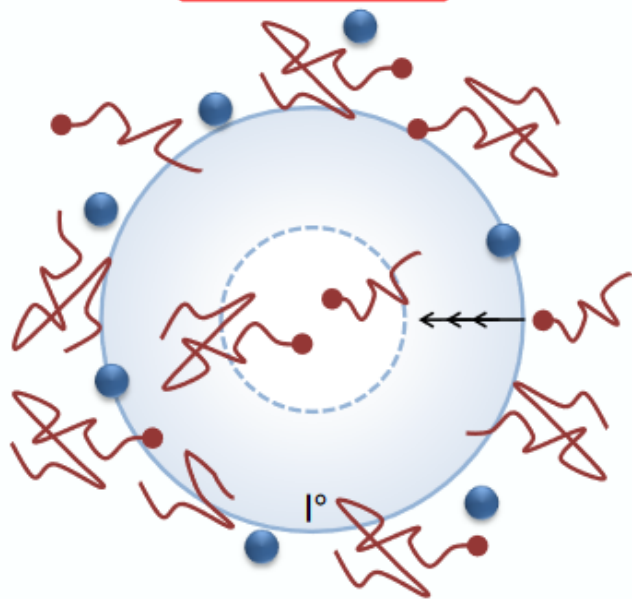
Termination



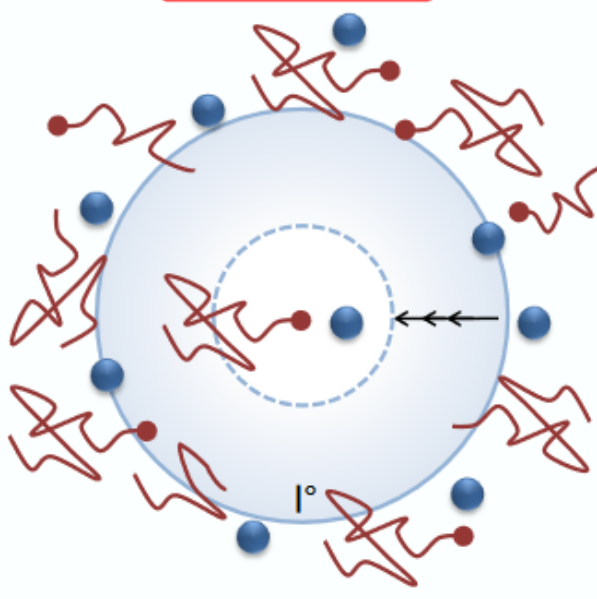


Diffusional limitations in FRP

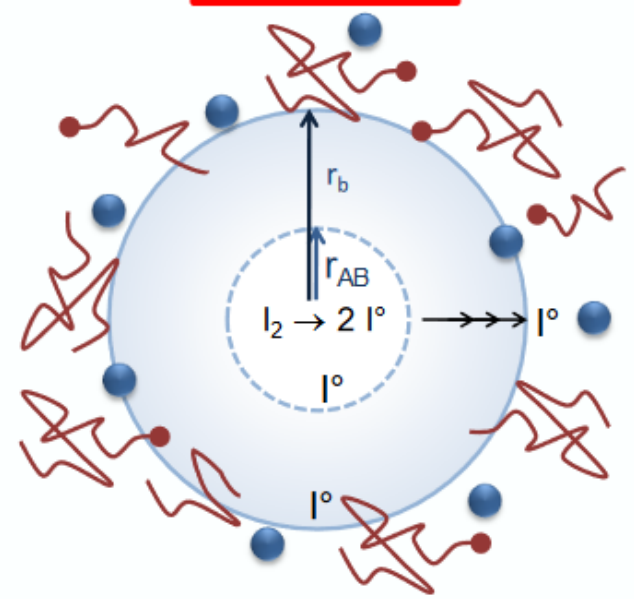
GEL EFFECT



GLASS EFFECT



CAGE EFFECT





Glass effect

Parallel encounter pair model

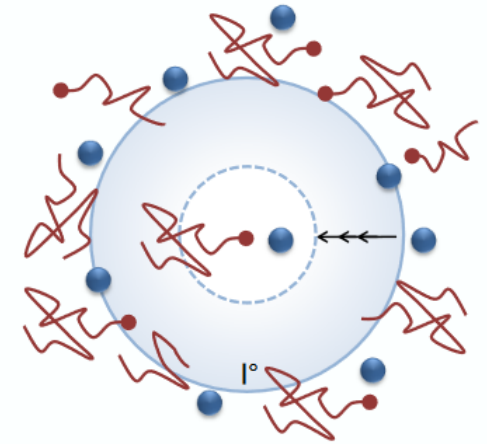
$$\frac{1}{k_{p,app}^i} = \frac{1}{k_{p,chem}^i} + \frac{1}{k_{p,diff}^i}$$

Smoluchowski equation

$$k_{p,diff}^i = k_{p,diff} = 4\pi\sigma_p N_A D_{tr,M}$$

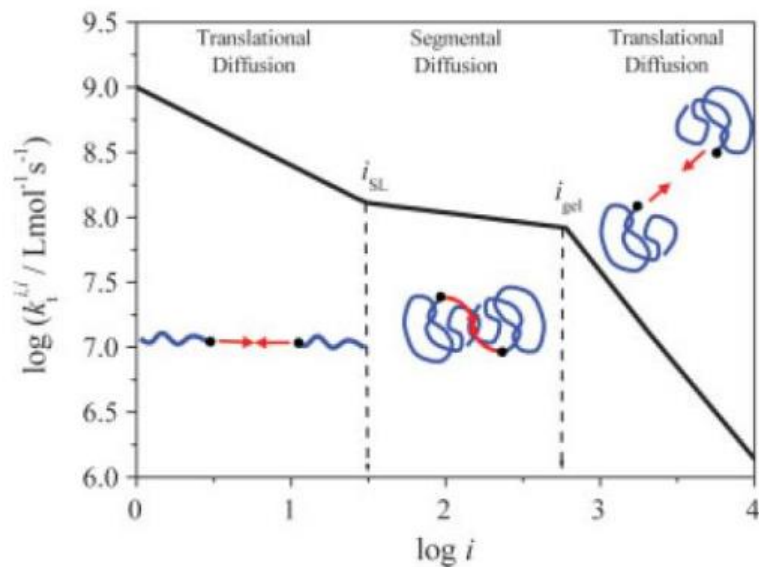
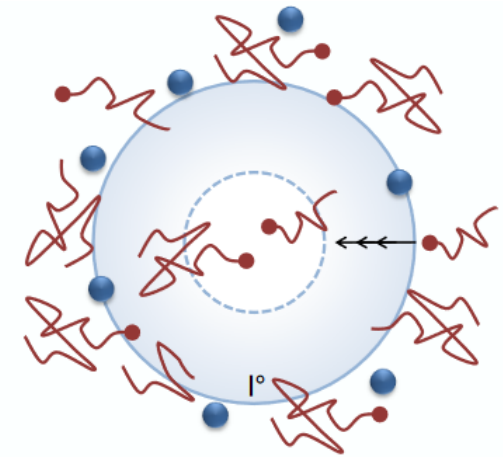
Free volume theory

$$D_{tr,M} = D_{M,0} e^{-\frac{E_{a,M}}{RT}} \left(-V_M^* M_{j,M} \frac{\frac{w_m}{M_{j,M}} + \frac{w_p}{M_{j,M}}}{V_{FH}/\lambda} \right)$$





Gel effect



$$\text{for } i < i_{\text{gel}} \text{ and } i < i_{\text{SL}}: k_{t,ii}^{\text{app}} = k_{t,11}^{\text{app}} i^{-\alpha_s}$$

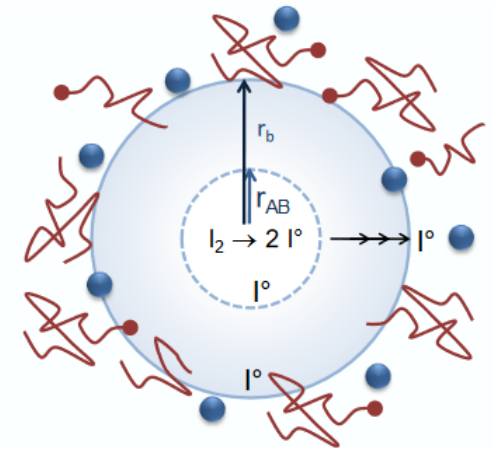
$$\text{for } i < i_{\text{gel}} \text{ and } i \geq i_{\text{SL}}: k_{t,ii}^{\text{app}} = k_{t,11}^{\text{app}} i_{\text{SL}}^{\alpha_1 - \alpha_s} i^{-\alpha_1}$$

$$\text{for } i \geq i_{\text{gel}} \text{ and } i < i_{\text{SL}}: k_{t,ii}^{\text{app}} = k_{t,11}^{\text{app}} i_{\text{gel}}^{\alpha_{\text{gel}} - \alpha_s} i^{-\alpha_{\text{gel}}}$$

$$\text{for } i \geq i_{\text{gel}} \text{ and } i \geq i_{\text{SL}}: k_{t,ii}^{\text{app}} = k_{t,11}^{\text{app}} i_{\text{SL}}^{\alpha_1 - \alpha_s} i_{\text{gel}}^{\alpha_{\text{gel}} - \alpha_1} i^{-\alpha_{\text{gel}}}$$



Cage effect



Apparent initiator efficiency as a function of monomer conversion

$$f_{app} = \frac{D_I}{D_I + D_{term}}$$

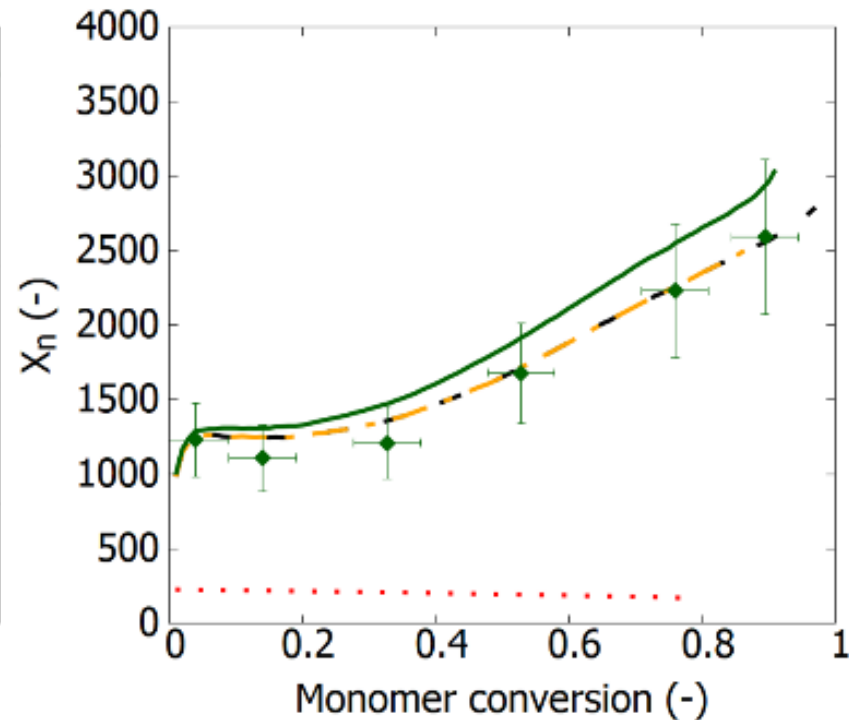
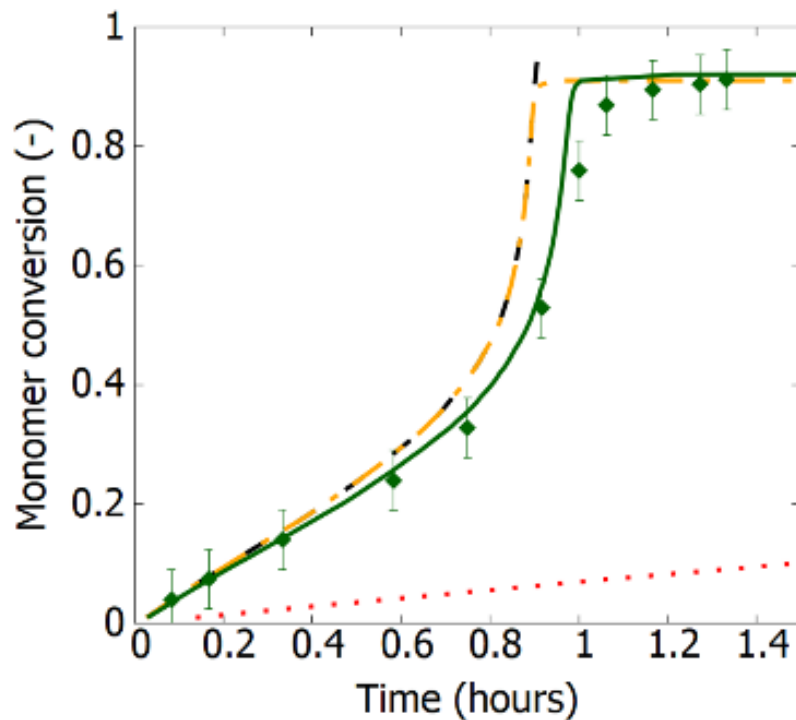
Free volume theory

$$D_I = D_{0,I} e^{-\frac{E_{a,I}}{RT}} \left(- \frac{w_m V_m^* \xi_{cp} / \xi_{mp} + w_p V_p^* \xi_{cp}}{V_{FH} / \lambda} \right)$$



Importance diffusional limitations in FRP

..... Intrinsic - - - - + gel effect - - - - + glass effect ——— + cage effect





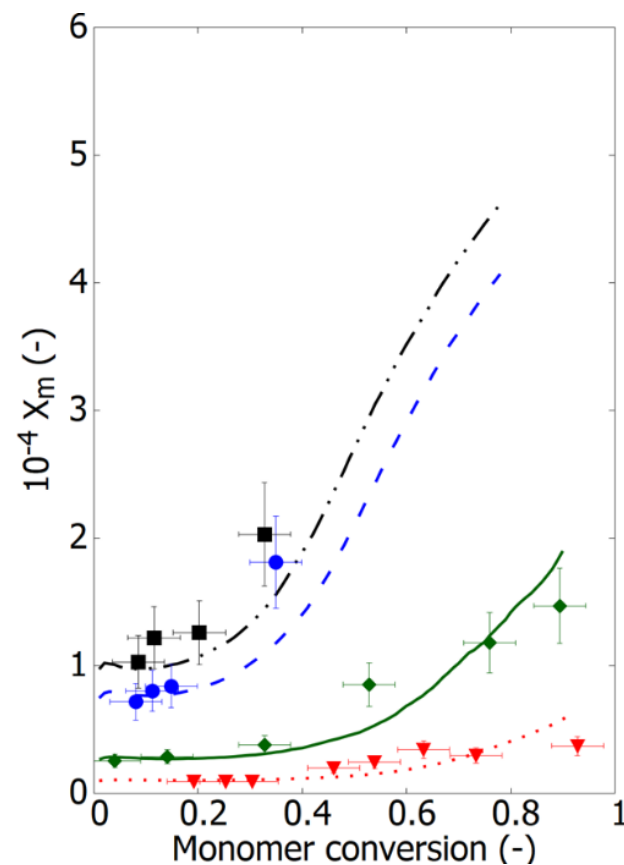
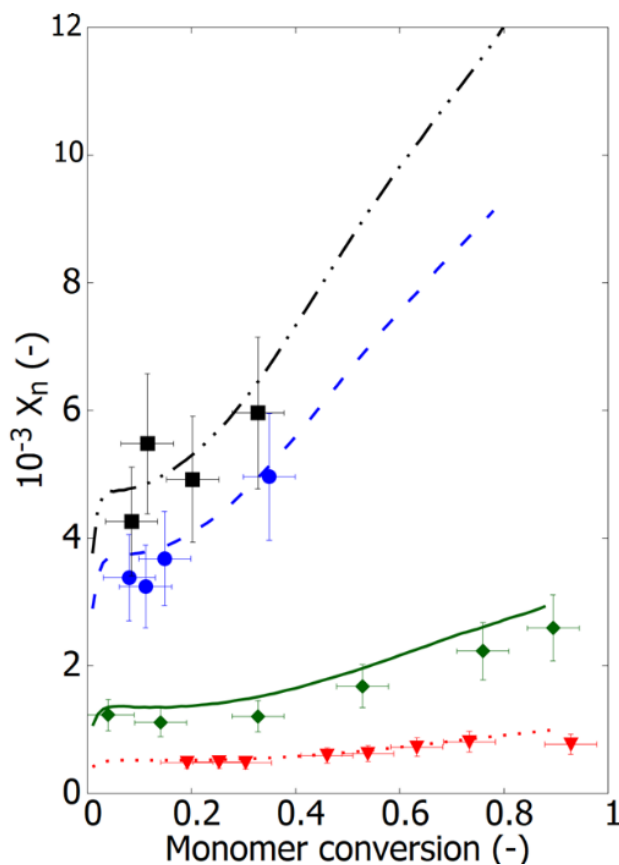
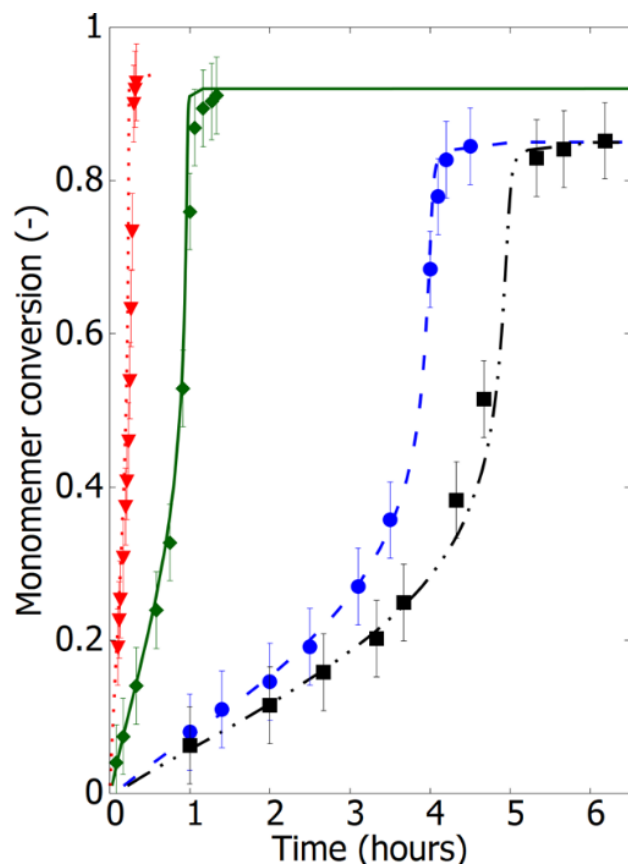
Model validation FRP

363 K and $[AIBN]_0:[MMA]_0=0.003$

343 K and $[AIBN]_0:[MMA]_0=0.003$

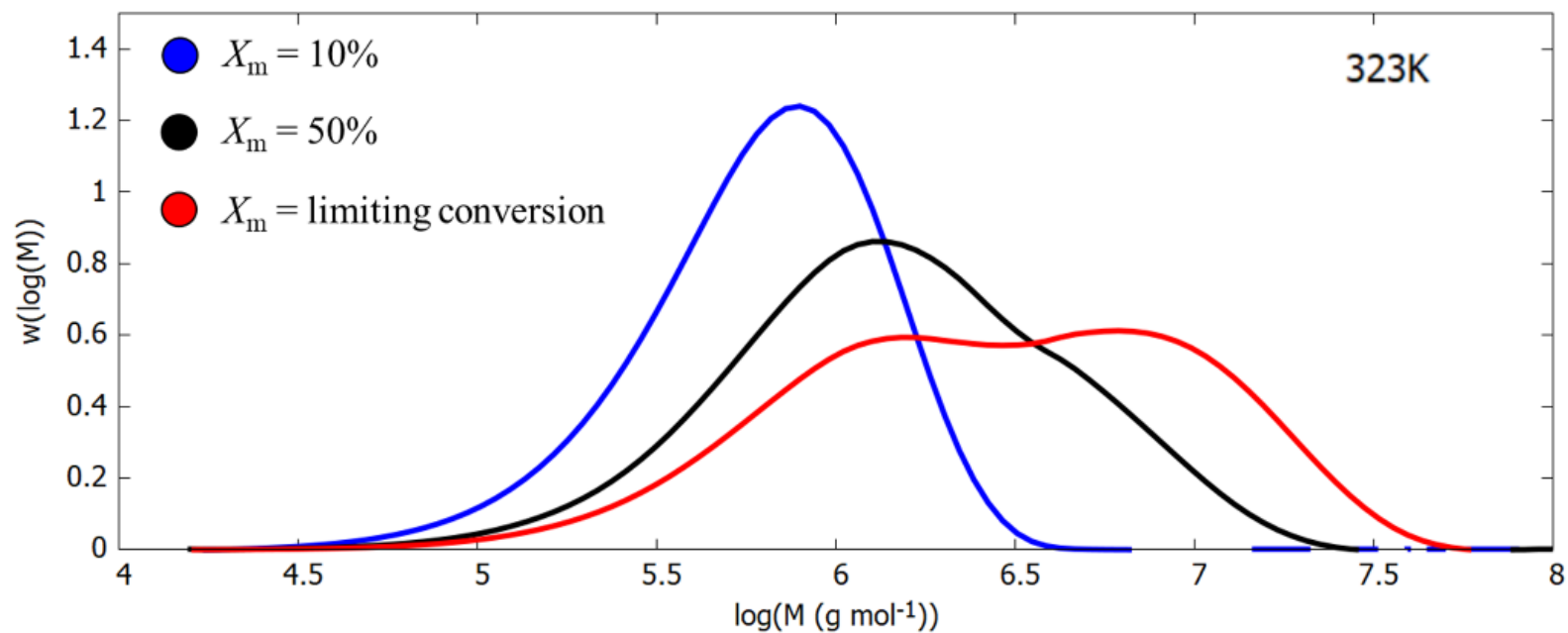
323 K and $[AIBN]_0:[MMA]_0=0.003$

323 K and $[AIBN]_0:[MMA]_0=0.002$



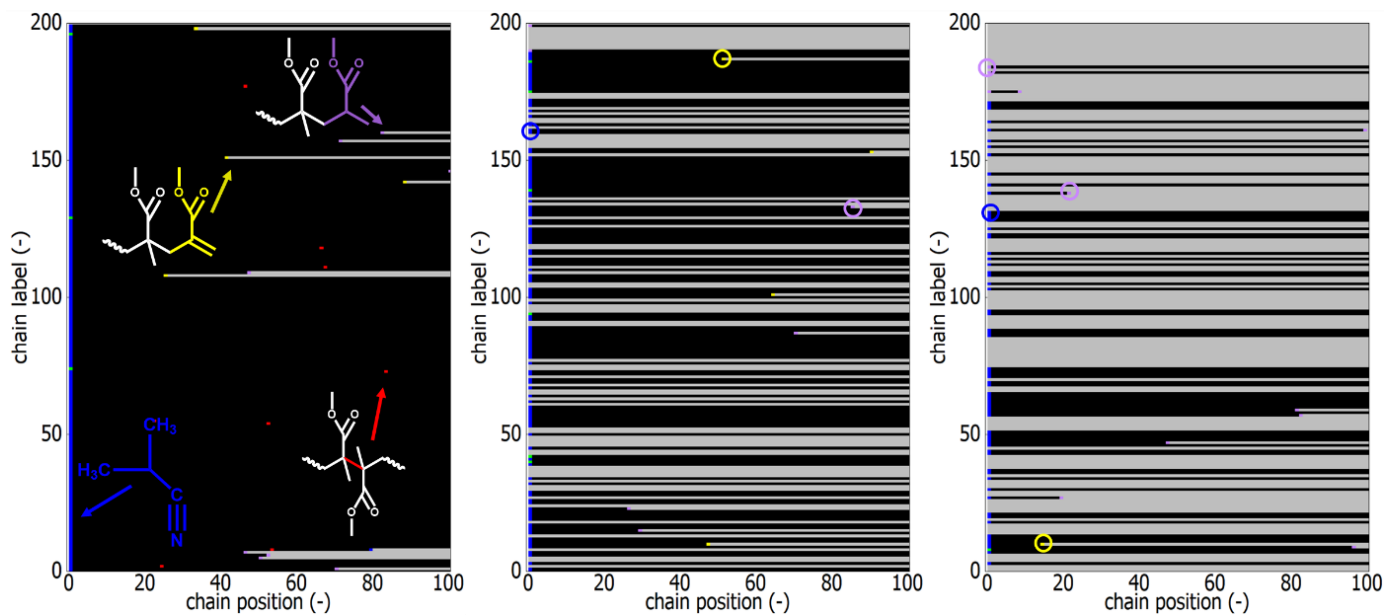
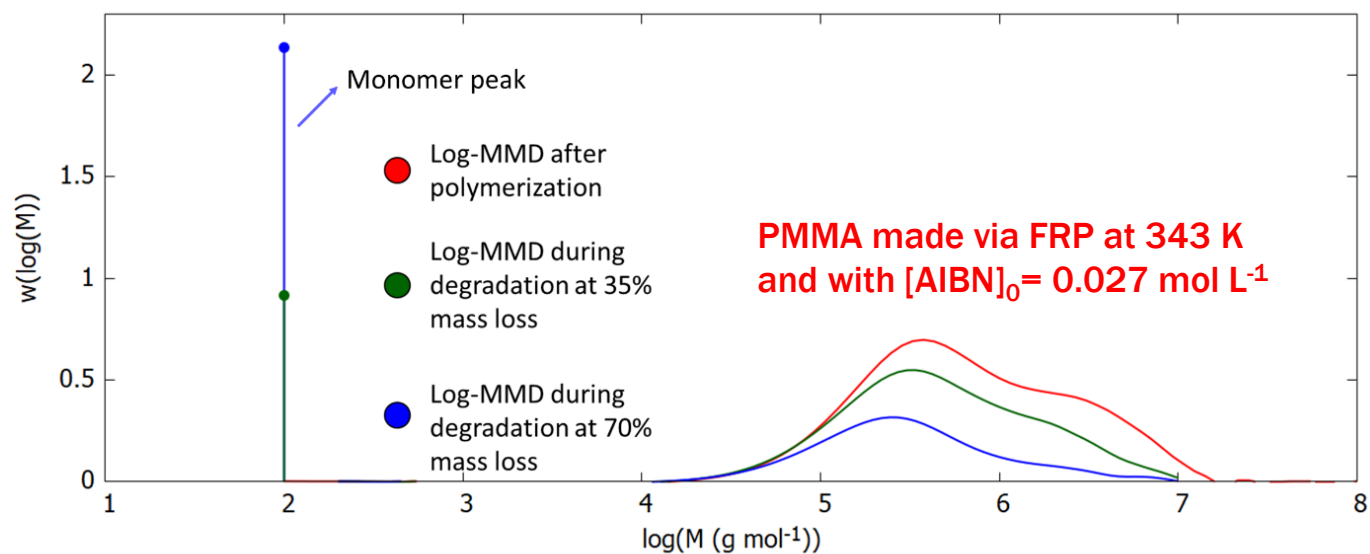


log-MMD evolution FRP





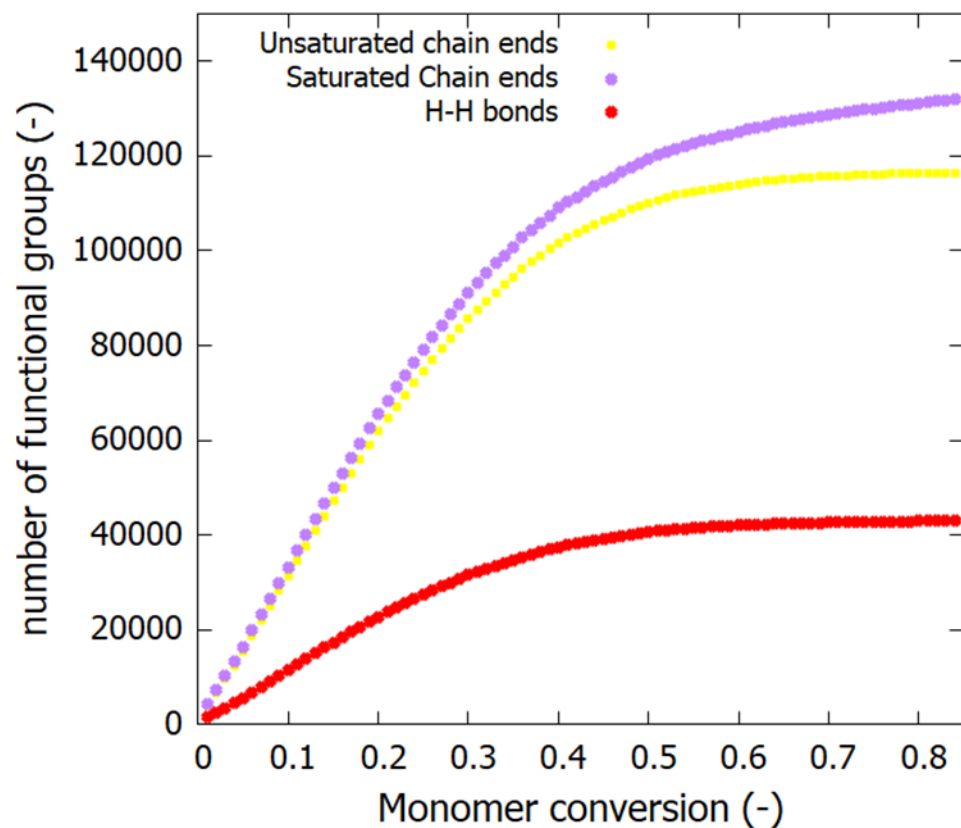
Depolymerization at 625 K



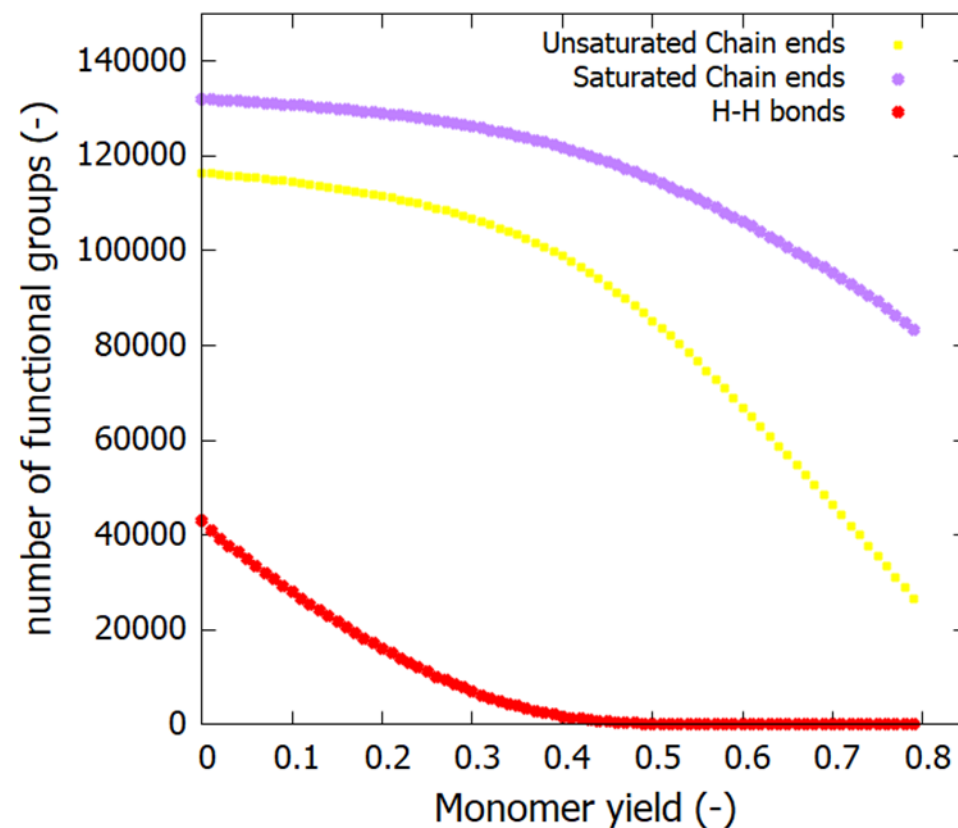


Evolution of functionalities

Polymerization



Depolymerization



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Conclusions

- **Chemical recycling** (depolymerization) allows to recover monomeric building blocks
- Depolymerization processes are characterized by a **large number of competing elementary reactions** such as fission, scission and termination reactions
- **Elementary reaction step based models** are key to improve the knowledge of depolymerization mechanisms and kinetics
- **Matrix based kinetic Monte Carlo** tools allow to track individual chains during both polymerization and depolymerization
- The initial **molar mass distribution** and the presence of **defects and functionalities** strongly affect the depolymerization kinetics



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